

No.6

大域照明

Global illumination

担当教員：向川康博・田中賢一郎

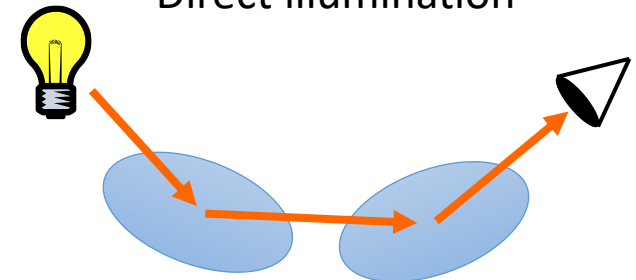
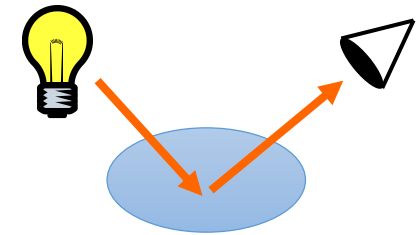
# Direct and global illuminations

## ■ Direct illumination

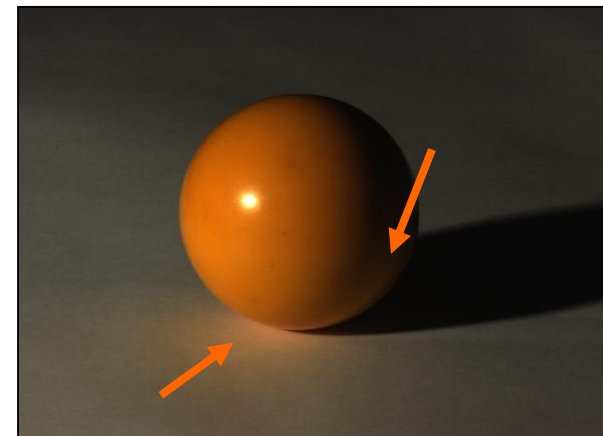
□ Light source → Object surface → Observer

## ■ Global (indirect) illumination

□ Light source → Object surface →  
Object surface → ... → Observer



Differences in CG (wikipedia)



Real global illumination

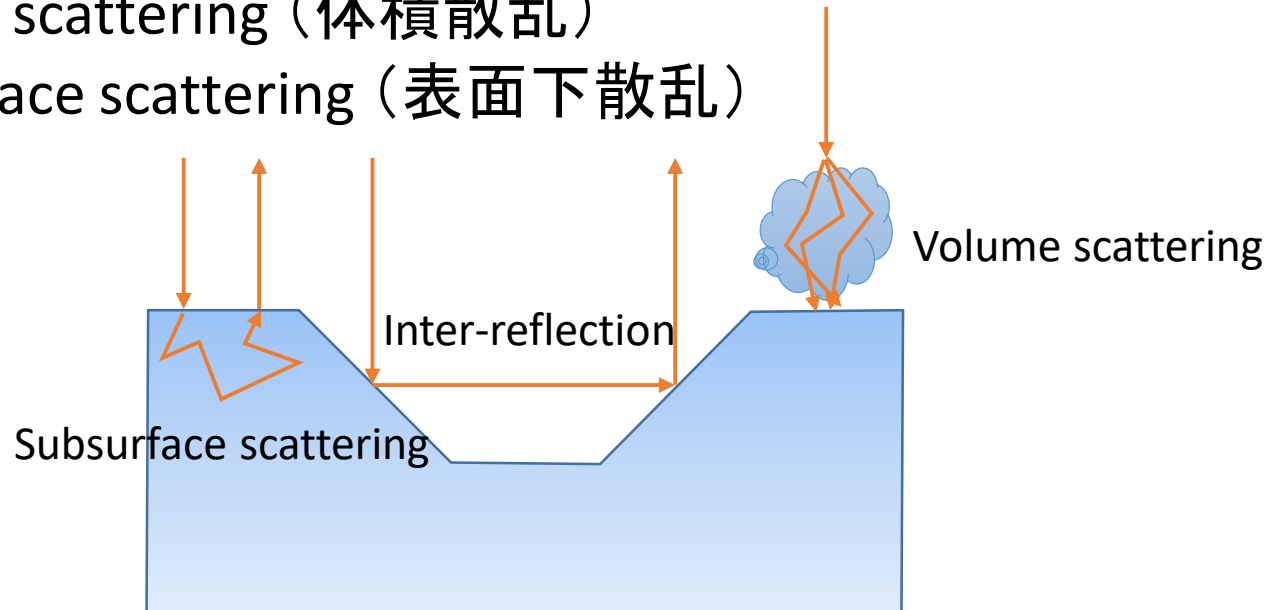
mini-report1: What is the difference?

# What is global illumination?

- Rendering images considering global illumination
  - ▣ In CG, necessary to render realistic image
  - ▣ In CV, necessary to analyze real scene

## ■ Types of global illumination

- ▣ Inter-reflection (相互反射)
- ▣ Volume scattering (体積散乱)
- ▣ Subsurface scattering (表面下散乱)



# Report

■ What is the difference of direct and global components?  
Explain from the following viewpoints.

- Optical phenomena (光学現象)
- Spatial frequency (空間的な周波数)
- Simplicity for modeling (モデル化の容易さ)



Direct component



Global component

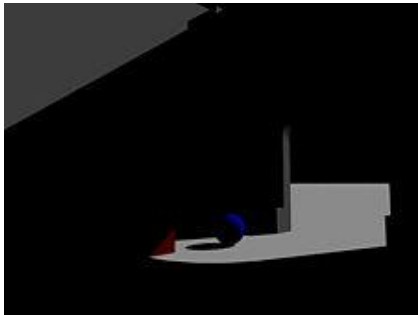
# Inter-reflection (相互反射)

# Inter-reflection

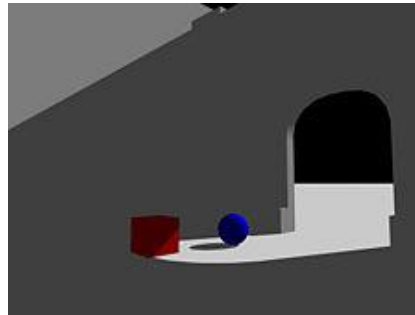
## ■ Diffuse inter-reflection

### □ Radiosity

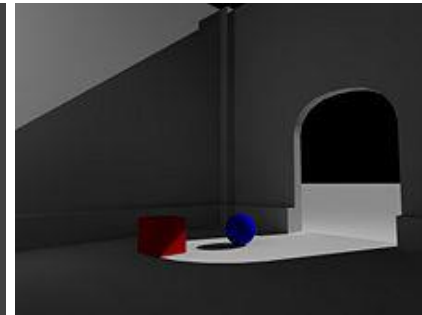
- Describing light passing between object surfaces by finite element method



Only direct illumination



Direct illumination  
+ ambient illumination



Radiosity

wiki.povray.org

## ■ Specular inter-reflection

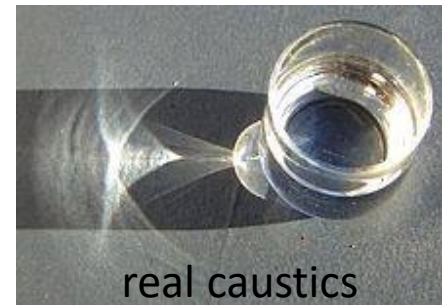
- Expression of caustics (集光模様)

- Monte Carlo ray tracing

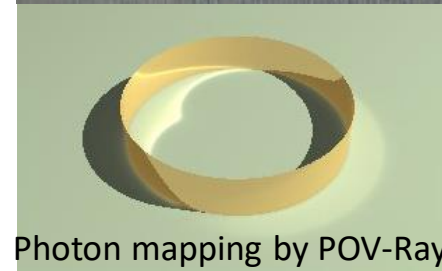
- Monte Carlo sampling from ray tracing

- Photon mapping

- Two-pass algorithm of distributing and counting photons



real caustics



Photon mapping by POV-Ray

# Radiosity

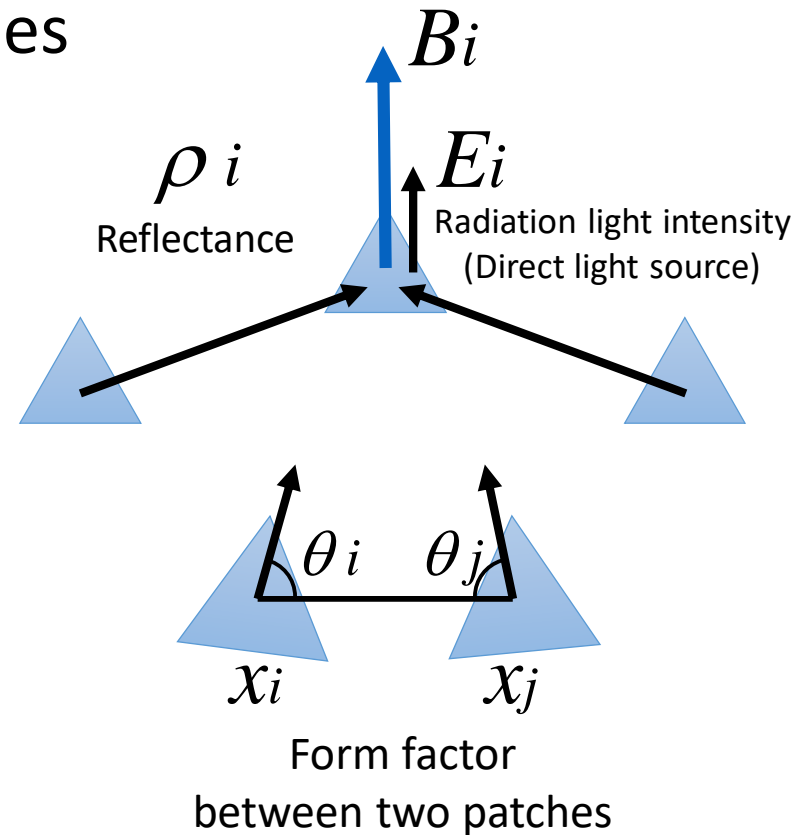
- Compute diffuse inter-reflection components
- Developed for heat transfer at first
- Form factor between two patches

$$B_i = E_i + \rho_i \sum_j F_{ij} B_j$$

$$F_{ij} = \underbrace{V(x_i, x_j)}_{\text{Visibility}} \underbrace{G(x_i, x_j)}_{\text{Geometric attenuation}}$$

(Can see each other or not)

$$G(x_i, x_j) = \frac{\cos \theta_i \cos \theta_j}{|x_i - x_j|}$$

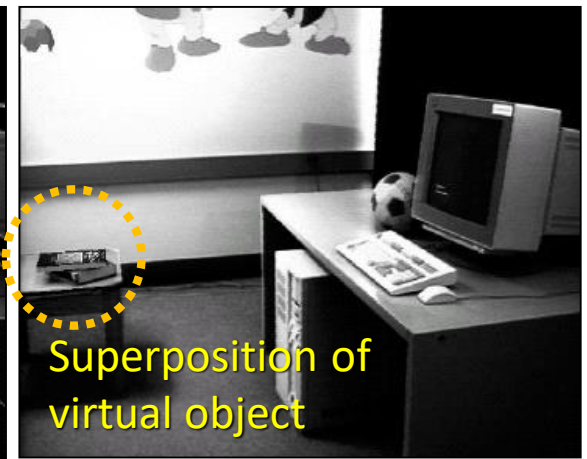
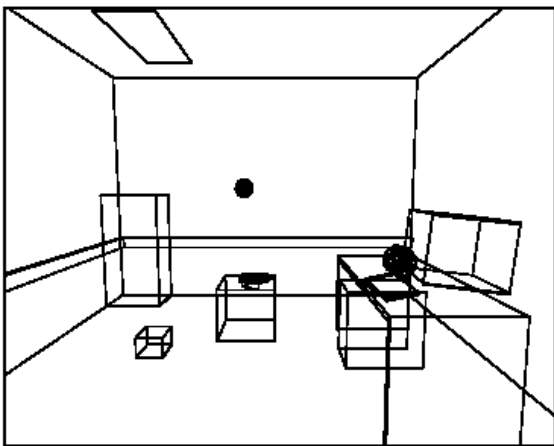


# Scene analysis based on Radiosity

- Reflectance estimation considering diffuse inter-reflection
- Simple linear solution

$$B_i = E_i + \rho_i \sum_j F_{ij} B_j$$

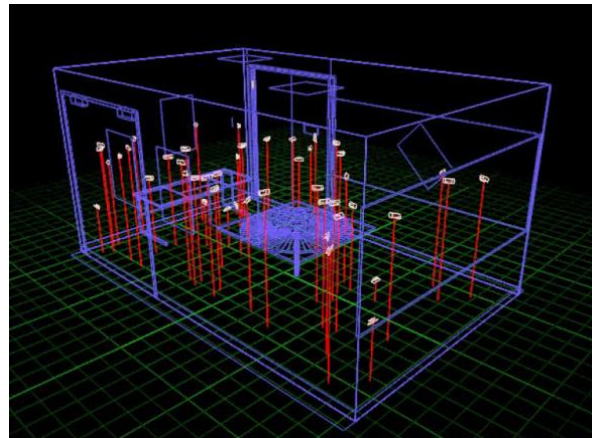
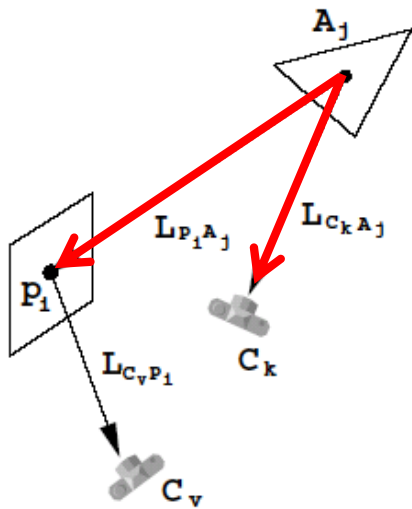
$$\rho_i = (B_i - E_i) / \sum_j F_{ij} B_j$$



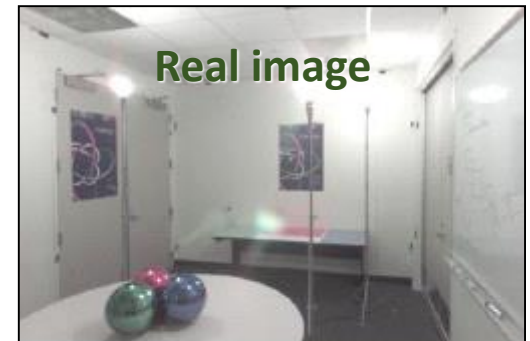


# Specular inter-reflection

- Specular reflection depends on viewing direction
- The radiance of each patch can not be directly observed
- Iterative computation of
  - radiance of one-bounce specular reflection
  - specular reflectance



Room shape and  
Camera position (40 places)



Yu et al., Inverse Global Illumination:

Recovering Reflectance Models of Real Scenes from Photographs, SIGGRAPH'99

# Specular reflectance



Resynthesis under original illumination



Superimposition of seven virtual objects

# Photon mapping (Jensen 1996)

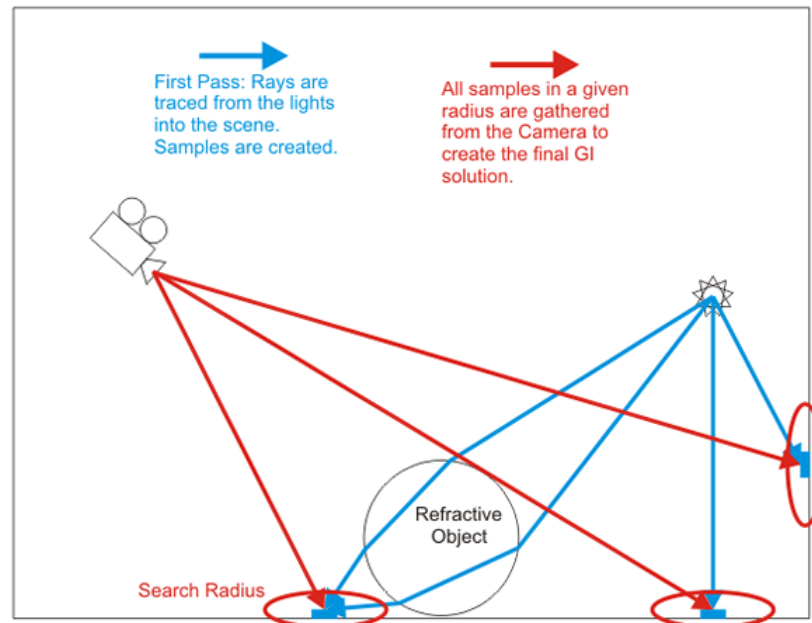
## ■ Two-pass algorithm to express global illumination

**1st pass:** Construction of photon map

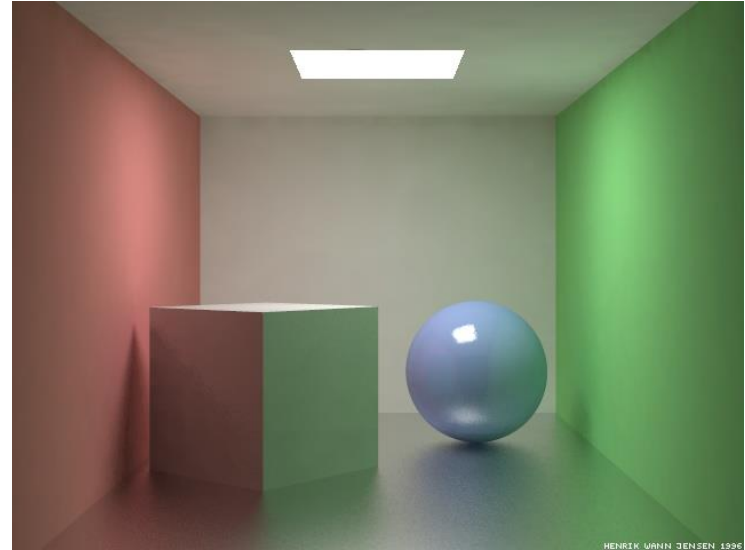
Distribute many photons from light

**2nd pass:** Rendering

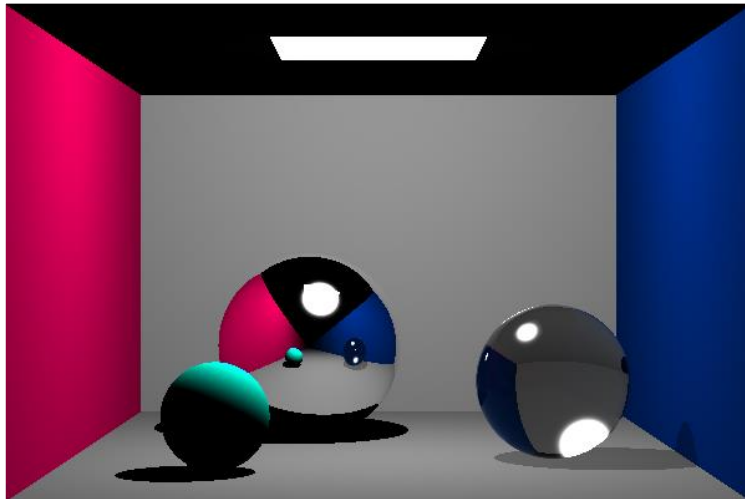
Count photons by ray tracing from viewpoint



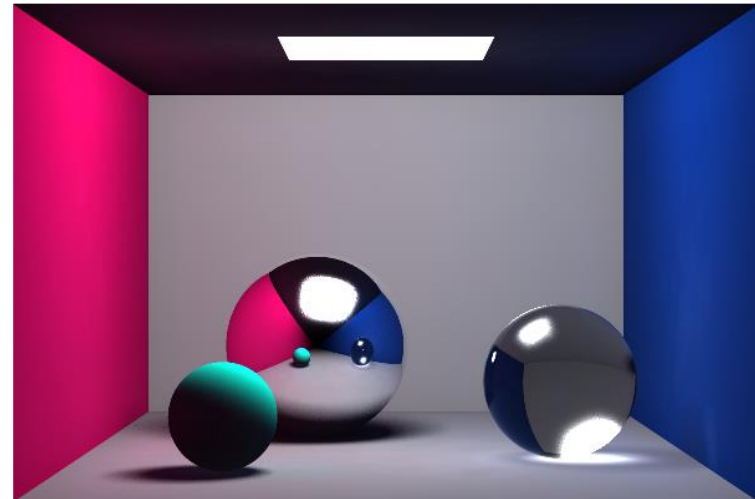
# Examples of photon mapping



[ Jensen, Global Illumination using Photon Maps, 1996 ]



Simple ray tracing



Photon mapping

# Inter-reflection in complex scene

simple

## ■ Diffuse inter-reflection

- Radiosity based on heat transfer

## ■ Allowing specular reflection

- Only one-bounce specular reflection
- Uniform specular reflection
- Simple path

- Light source → Diffuse reflection → Specular reflection  
→ camera

## ■ Specular inter-reflection

- Iterative computation to fit input Photon mapping method
- Photon mapping

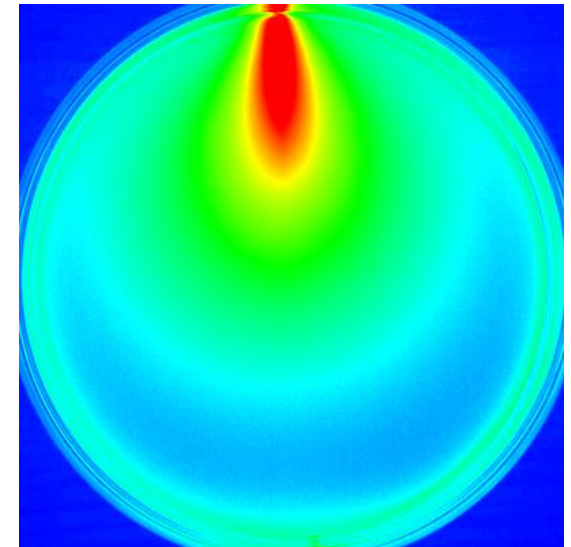
complex



# Volume Scattering (体積散乱)

# Scattering in translucent media

- How an incident ray repeats scattering and the light propagates in a translucent media?
  - Multiple bounces
  - Complex light field



dark

bright

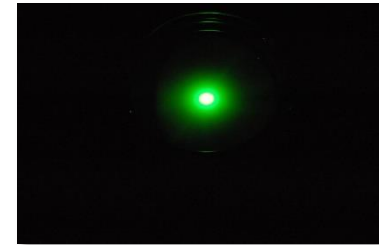
# Different scattering due to optical density



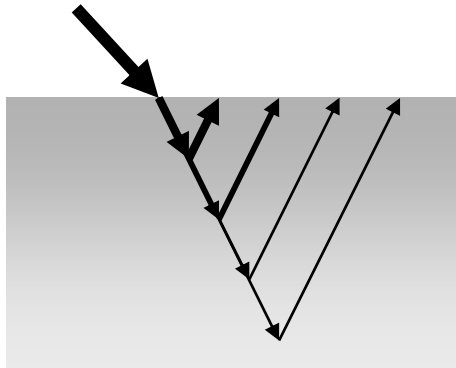
Vitamin water



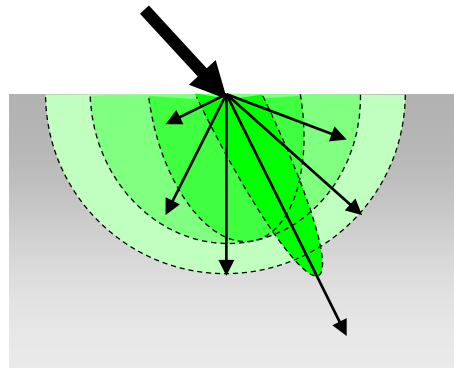
Orange juice



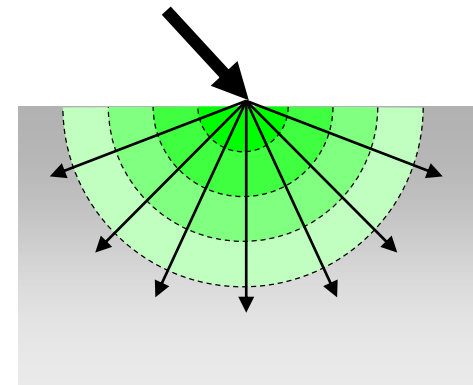
Milk



Single scattering



Low-order bounce scattering

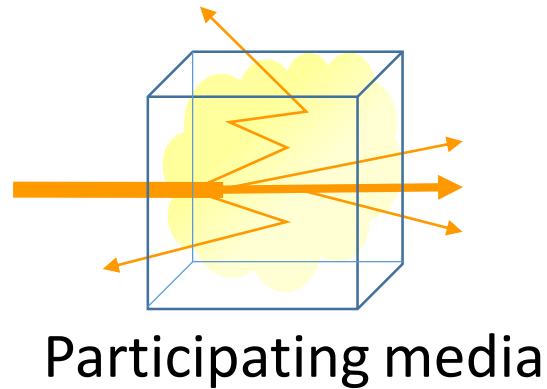
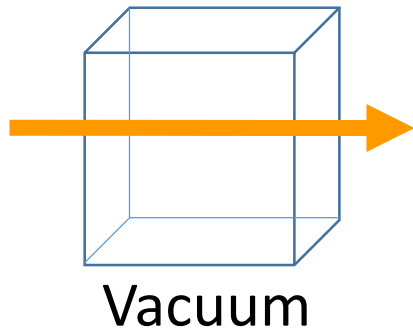


Multiple scattering  
(diffusion)



# Participating media (関与媒質)

- Consist of small particles
- Collision with particles



# Light transport in participating media

## ■ Absorption:

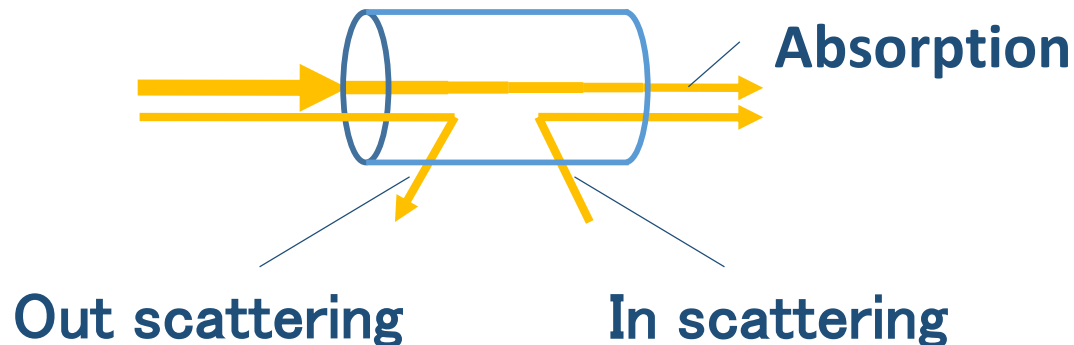
- Collision with particles
- **Decrease** in intensity

## ■ Out scattering:

- Scattered to outside
- **Decrease** in intensity

## ■ In scattering:

- Ray from outside scatters and joins to traveling direction
- **Increase** in intensity



# Energy decrement

## ■ Attenuation by absorption

$$dL(x, \omega) = -\sigma_a(x)L(x, \omega)ds \quad \sigma_a(x) : \text{Absorption coefficient [m}^{-1}\text{]}$$

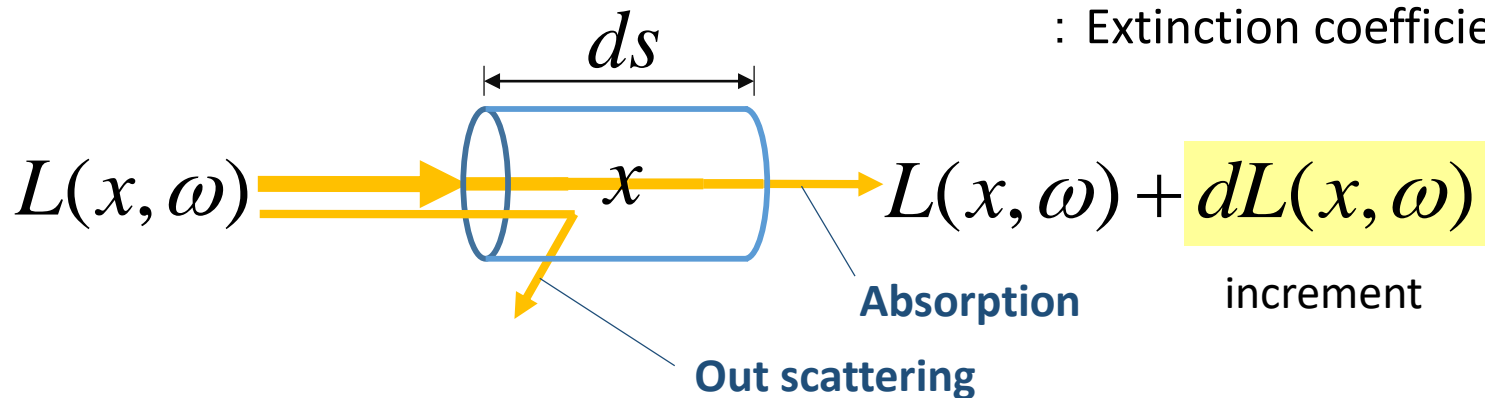
## ■ Attenuation by out scattering

$$dL(x, \omega) = -\sigma_s(x)L(x, \omega)ds \quad \sigma_s(x) : \text{scattering coefficient [m}^{-1}\text{]}$$

## ■ Summing both attenuations by absorption + out scattering

$$dL(x, \omega) = -\sigma_t(x)L(x, \omega)ds \quad \sigma_t(x) = \sigma_a(x) + \sigma_s(x)$$

: Extinction coefficient [m<sup>-1</sup>]



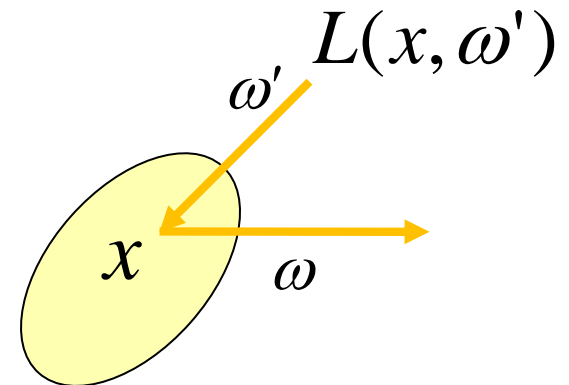
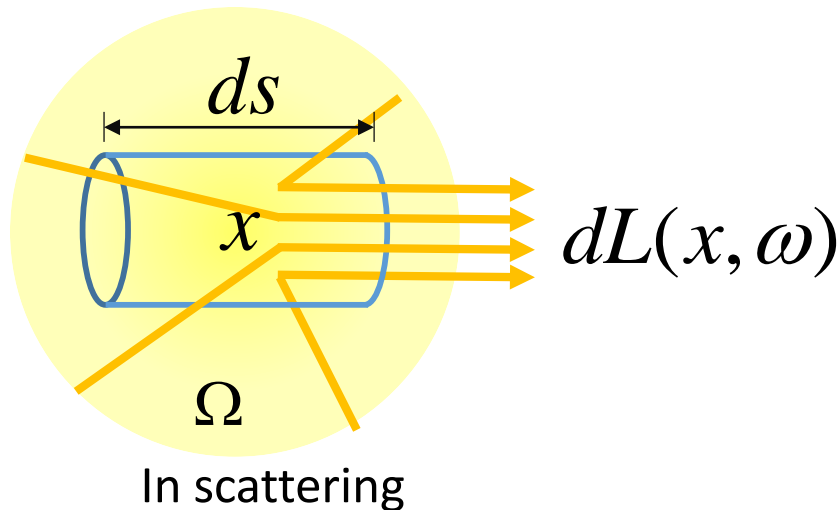
# Energy increment

## ■ Increment by in scattering

- Integrating rays coming from each direction  $\omega'$  of the spherical surface  $\Omega$  surrounding point  $x$

$$dL(x, \omega) = \sigma_s(x) \left( \int_{\Omega} p(x, \omega', \omega) L(x, \omega') d\omega' \right) ds$$

Phase function



# Phase function

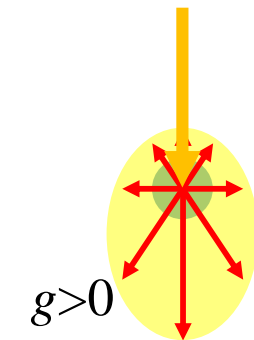
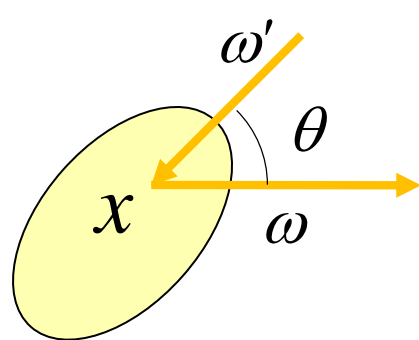
## ■ Expression of scattering bias

▣ depends only on the angle  $\theta$  between  $\omega$  and  $\omega'$  for most media

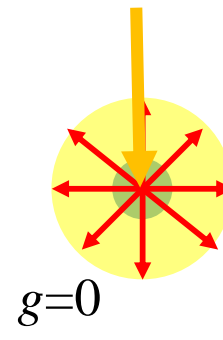
▣ Henyey-Greenstein function

▣  $g$ : scattering anisotropy

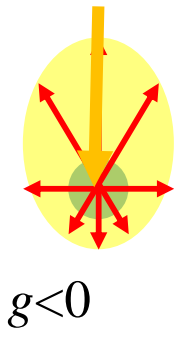
$$p(\theta) = \frac{1}{4\pi} \frac{1 - g^2}{(1 + g^2 - 2g \cos \theta)^{\frac{3}{2}}}$$



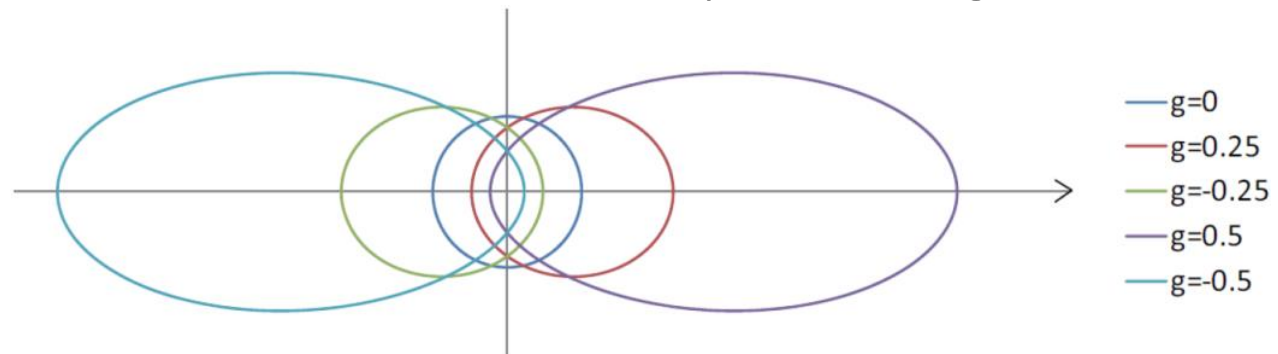
Forward scattering



Isotropic scattering

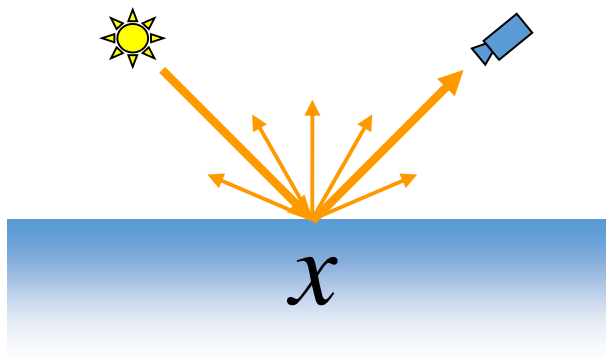
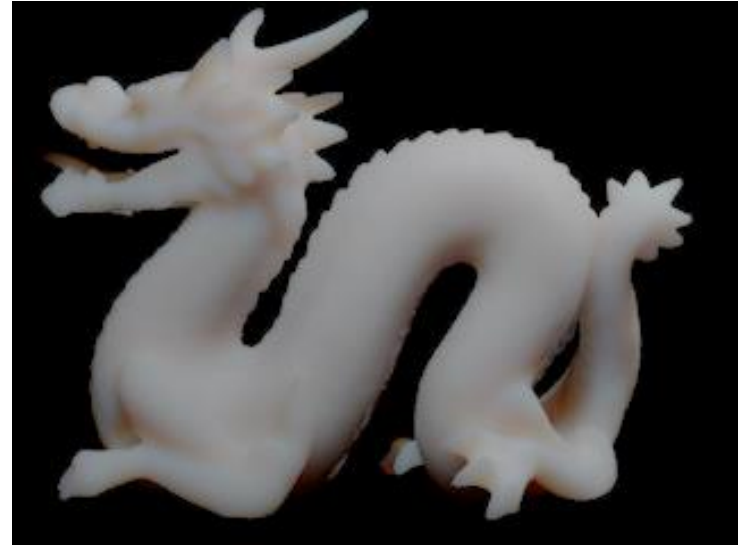
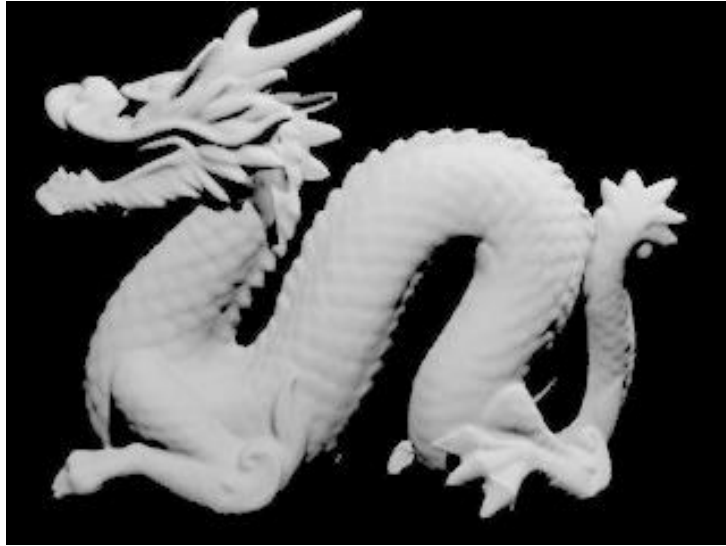


Back scattering

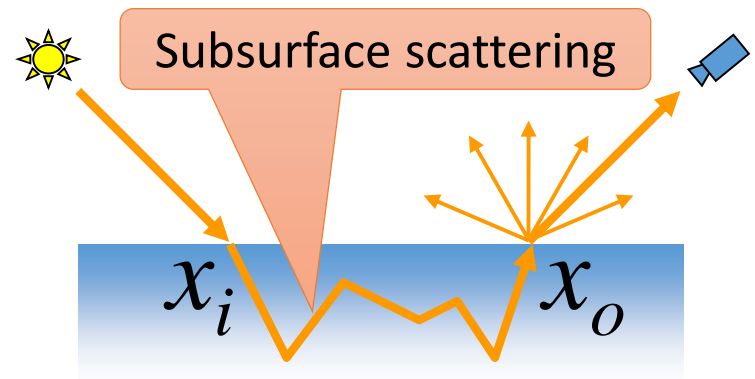


# Subsurface Scattering (表面下散乱)

# Subsurface scattering in translucent objects



Opaque (不透明)



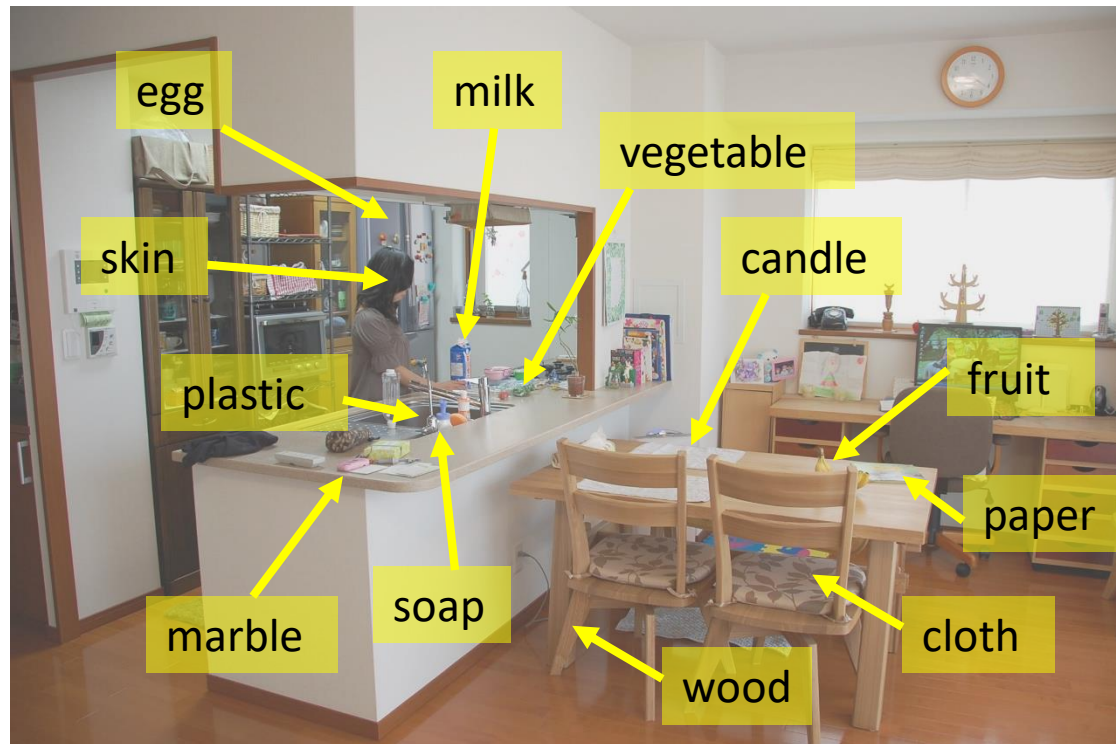
Translucent (半透明)

# Translucent objects are not special

- Typical translucent objects:

- marble, milk, and skin

- Most objects except for metal are translucent



Translucent objects in our daily environment



# Importance of subsurface scattering in CG

- Representation of realistic skin
- Especially necessary for rendering human image



**Jurassic Park (1993)**



**Dobby of " Harry Potter and the Chamber of Secrets " (2002)**  
(The first movie that computed physically accurate subsurface scattering)



**Gollum of "Lord of the Rings" (2002-2003)**

# Difference in scattering properties



# Different distribution



# BSSRDF (双方向散乱表面反射分布関数)

(**B**idirectional **S**cattering **S**urface **R**eflectance **D**istribution **F**unction)

- How much the incident light at a point  $x_i$  from a direction  $(\theta_i, \phi_i)$  outgoing from a point  $x_r$  to a direction  $(\theta_r, \phi_r)$
- The difference with BRDF is that the incident and outgoing exit points are different.

## ■ Opaque object

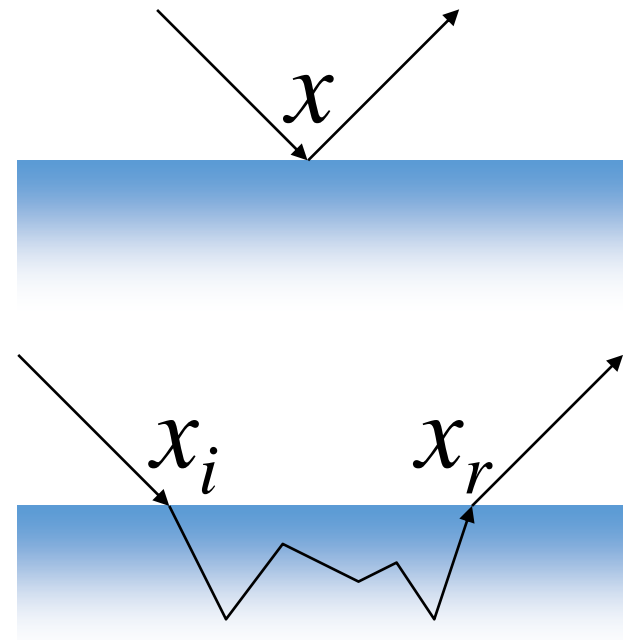
- locally defined

$$f_{BRDF}(x, \theta_i, \phi_i, \theta_r, \phi_r)$$

## ■ Translucent object

- globally defined

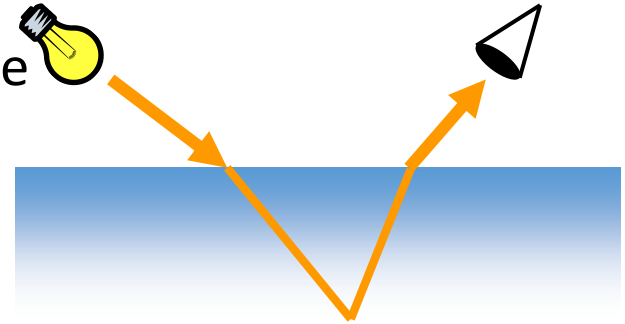
$$f_{BSSRDF}(x_i, \theta_i, \phi_i, x_r, \theta_r, \phi_r)$$



# Single scattering and Multiple scattering

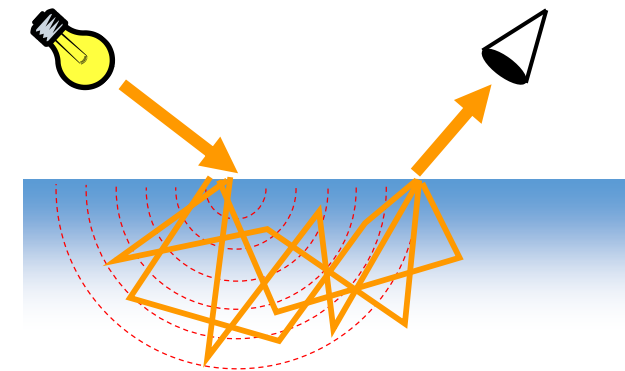
## ■ Single scattering :

- Collision with a particle **only once** inside the medium
- Observed in optically thin medium
  - such as milky water, fog,...
- High directivity and uniquely determined light path



## ■ Multiple scattering :

- Repeat reflections **many times** inside the medium
- Observed in optically dense medium
  - such as skin, marble, milk,...
- **Diffusion approximation**

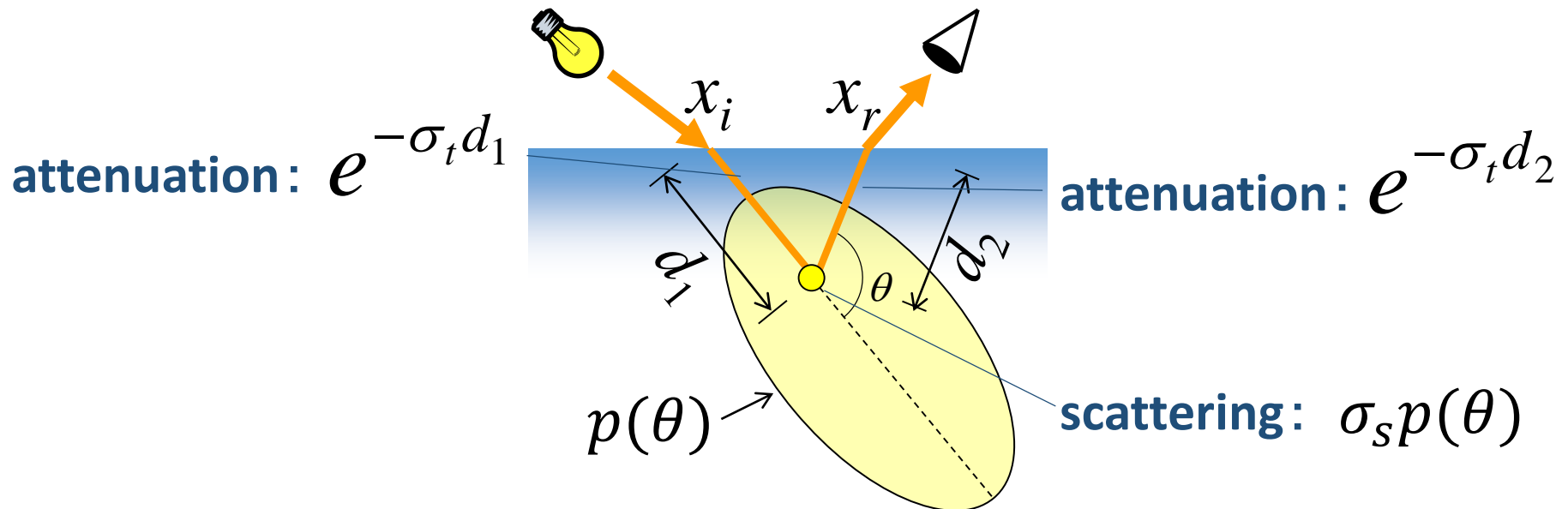


# Model of single scattering

## ■ Modeling the sequence of attenuation

→ scattering → attenuation

$$f_{BSSRDF}^{single}(x_i, \theta_i, \phi_i, x_r, \theta_r, \phi_r) = \sigma_s p(\theta) e^{-\sigma_t(d_1+d_2)}$$



# Model of multiple scattering

## ■ Direct tracing

- Monte Carlo ray tracing, photon mapping
- High computational cost, since reflections are repeated.

## ■ Approximated parametric function

- Diffusion approximation
- Dipole model (Jensen 2001) , multipole model (Donner 2005)



Multi-layered model



Dipole



Multi-layer

# Dipole Model for BSSRDF (Jensen et al. SIGGRAPH2001)

## ■ Decomposition of the BSSRDF

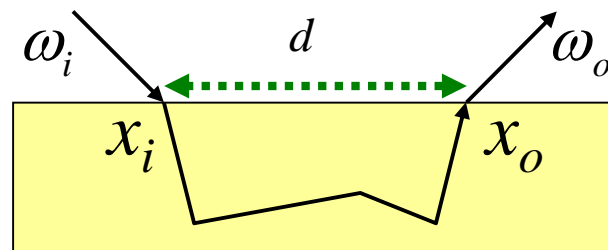
### □ Fresnel transmittance: $F_t(\eta, \omega)$

- function of relative index of refraction  $\eta$ , incident and reflective angles  $\omega_i$  and  $\omega_o$

### □ Diffuse BSSRDF: $R(d)$

- function of distance  $d$  between incident and outgoing points  $x_i$  and  $x_o$
- including two inherent parameters of the material
- scattering coefficient:  $\sigma_s$
- absorption coefficient:  $\sigma_a$

$$f_{BSSRDF}^{multiple}(x_i, \theta_i, \phi_i, x_r, \theta_r, \phi_r) = \frac{1}{\pi} \underbrace{F_t(\eta, \theta_i, \phi_i)}_{\text{Fresnel transmittance at } x_i} \underbrace{R_d(\|x_i - x_r\|)}_{\text{Diffuse BSSRDF}} \underbrace{F_t(\eta, \theta_r, \phi_r)}_{\text{Fresnel transmittance at } x_o}$$

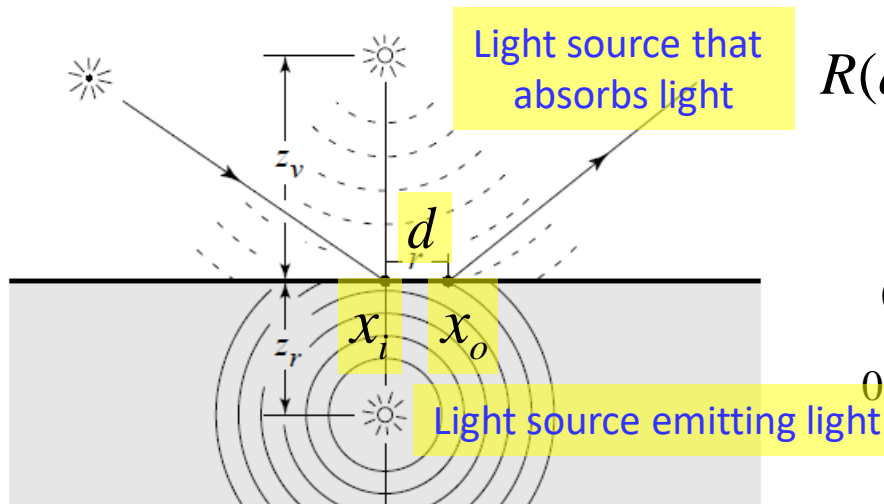




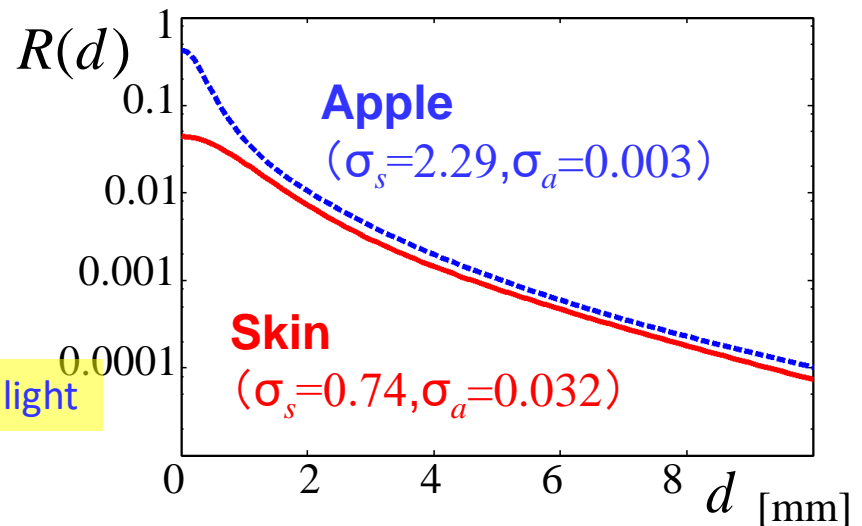
# Diffuse BSSRDF in Dipole model

- Assumption of diffusion approximation
- A point light source in object
- In order to satisfy the boundary condition, a negative light source above the incident point

$$R(d) = \frac{\alpha'}{4\pi} \left[ z_r (\sigma_{tr} d_r + 1) \frac{e^{-\sigma_{tr} d_r}}{\sigma'_t d_r^3} + z_v (\sigma_{tr} d_v + 1) \frac{e^{-\sigma_{tr} d_v}}{\sigma'_t d_v^3} \right]$$



Concept of dipole model



Examples of scattering terms

# Rendering example with dipole model

BRDF



BSSRDF



mini-report2: What is the difference?

Decomposition using  
high-frequency illumination  
(高周波照明による成分分解)

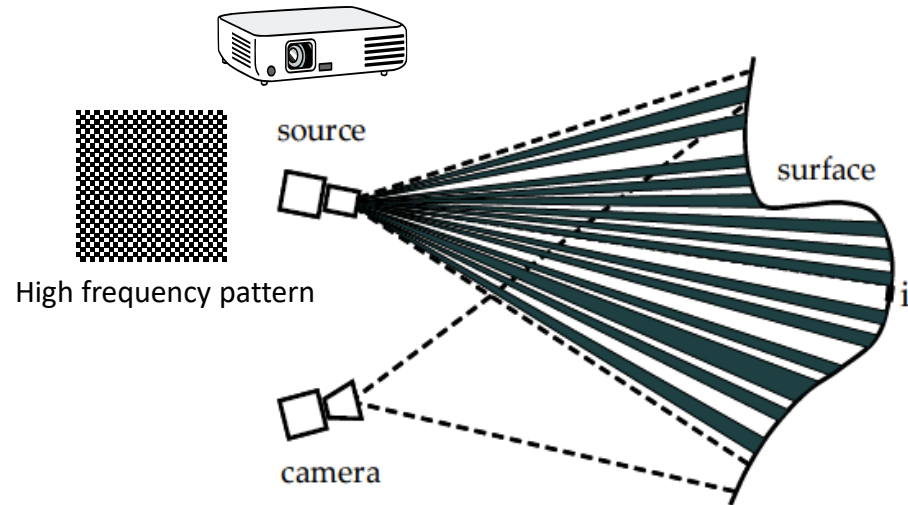
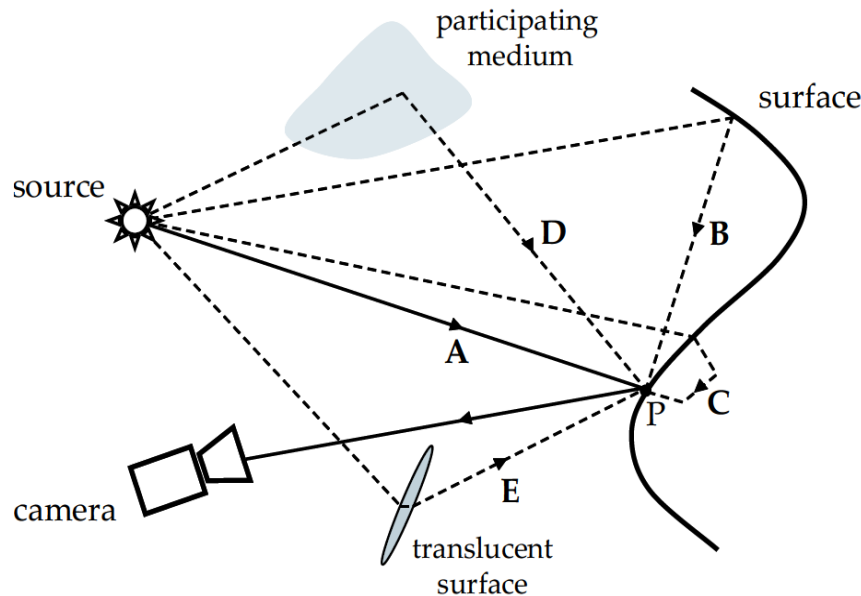
# Decomposition of Global Illumination(Nayar 2006)

## ■ Separation of two components

- ▣ Direct component (diffuse reflection / specular reflection)
- ▣ Global components (inter-reflection, volume scattering, subsurface scattering ...)

## ■ Using a projector as a light source

- ▣ Projecting high frequency pattern (fine grid pattern)
- ▣ Utilizing that the global illumination effect acts as a low-pass filter



# Principle of high frequency illumination

## ■ When not illuminated :

- Global component / 2

- White pixels and black pixels mix  
- Half is white in the projection pattern

## ■ When illuminated :

- Direct component + Global component / 2

## ■ Separation of two components

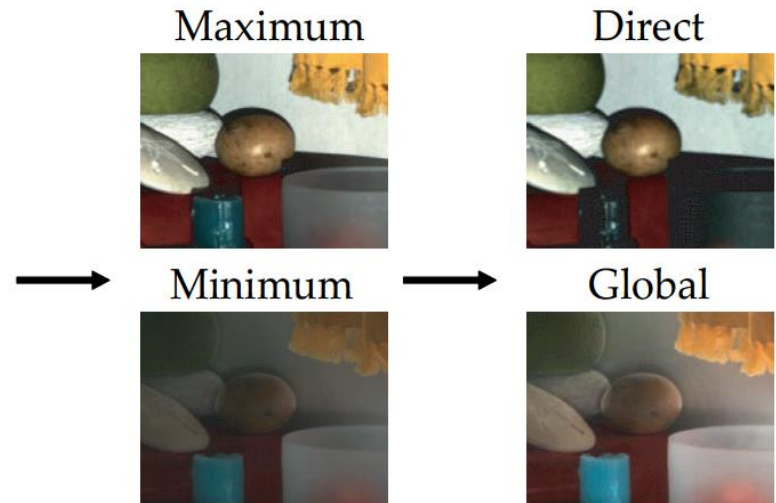
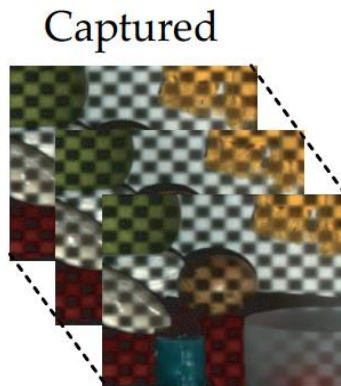
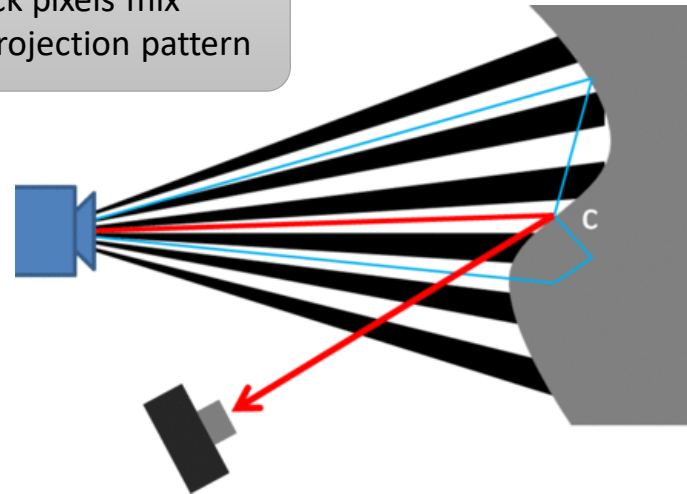
$$\max = \text{direct} + \frac{1}{2} \text{global}$$

$$\min = \frac{1}{2} \text{global}$$

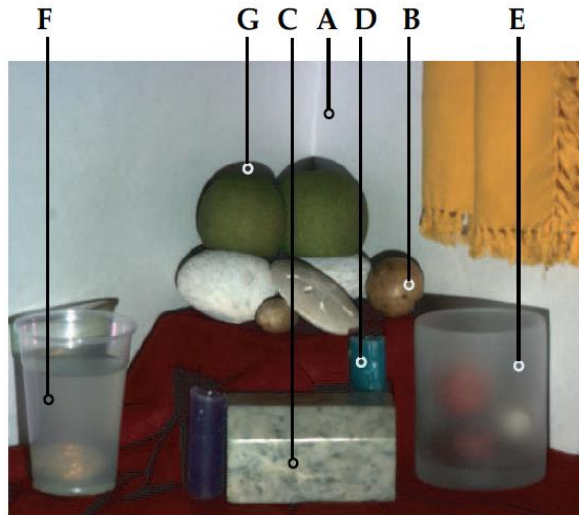


$$\text{direct} = \max - \min$$

$$\text{global} = 2 \min$$



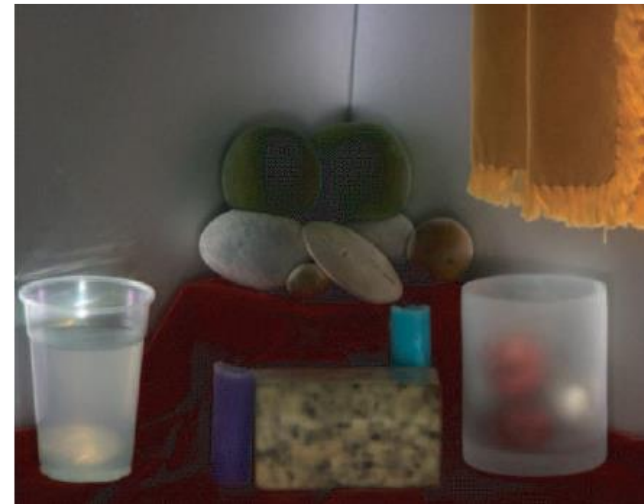
# Decomposition of direct and global components



- A: Diffuse Interreflection (Board)
- B: Specular Interreflection (Nut)
- C: Subsurface Scattering (Marble)
- D: Subsurface Scattering (Wax)
- E: Translucency (Frosted Glass)
- F: Volumetric Scattering (Dil. Milk)
- G: Shadow (Fruit on Board)



Direct component



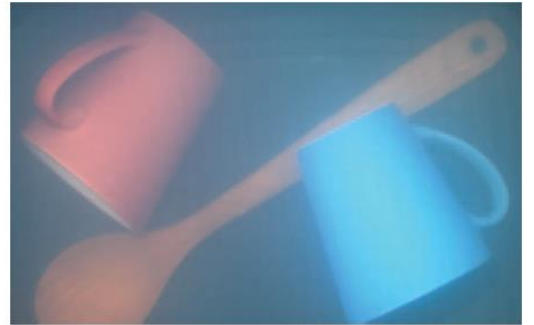
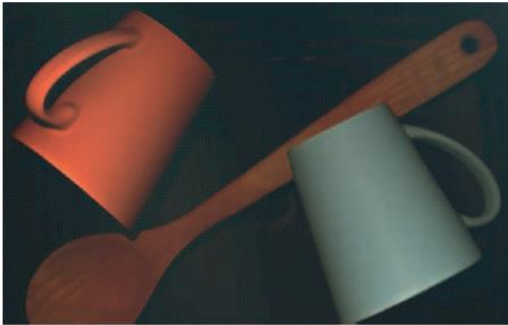
Global component

# Decomposition of direct and global components

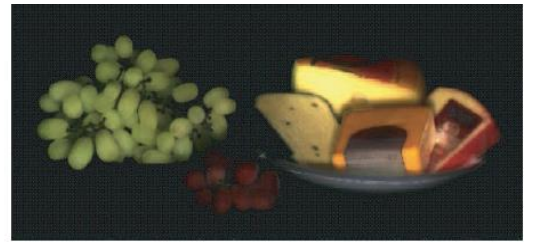
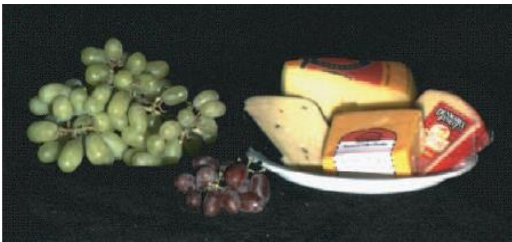
Inter-reflection



Volume scattering



Subsurface scattering



Original scene

Direct component

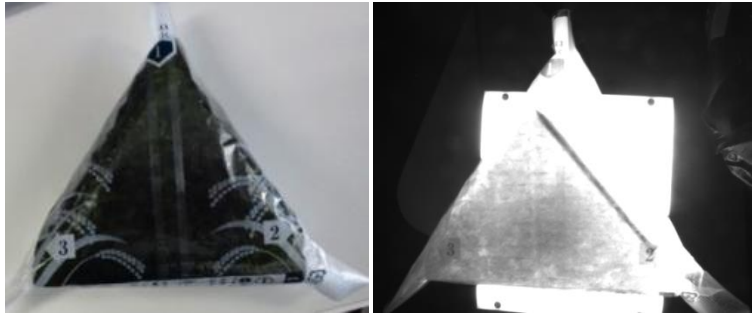
Global component

Decomposition of  
transmissive lights  
(透過光の分解)

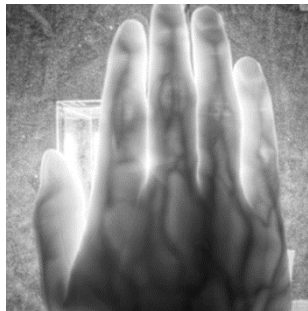


# Visualization using IR light

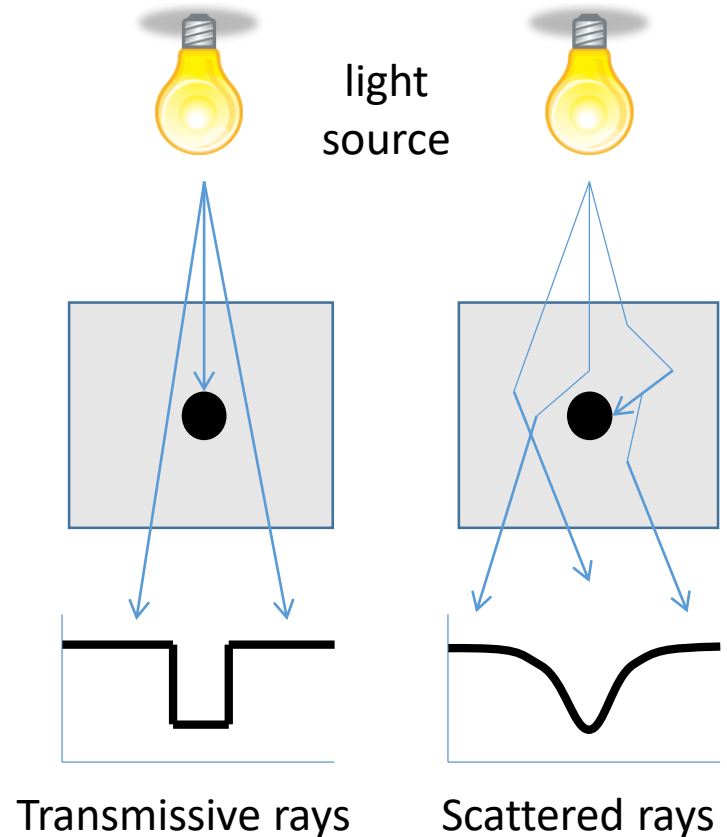
- Transmissive image using IR light.
- Unclear image due to *scattering*.



Metal object in food



Vein pattern



# Transmissive high frequency illumination

(ICCP2013)

- Decomposition of transmissive and scattered rays.
- Parallel high frequency illumination
  - When phase change,
    - **transmissive**: change
    - **scattered**: no change

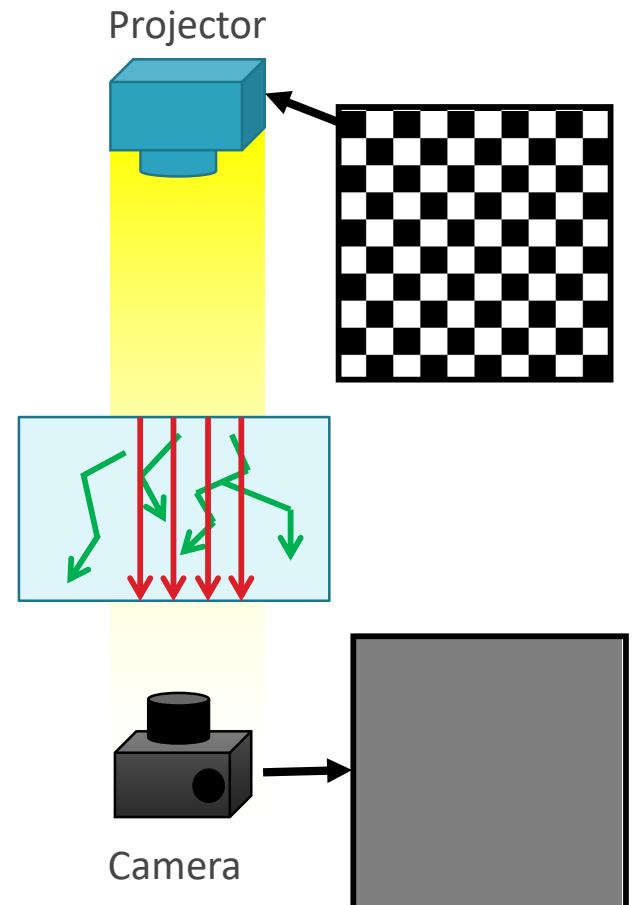
## ■ Decomposition

$$max = transmissive + \frac{1}{2} scattered$$

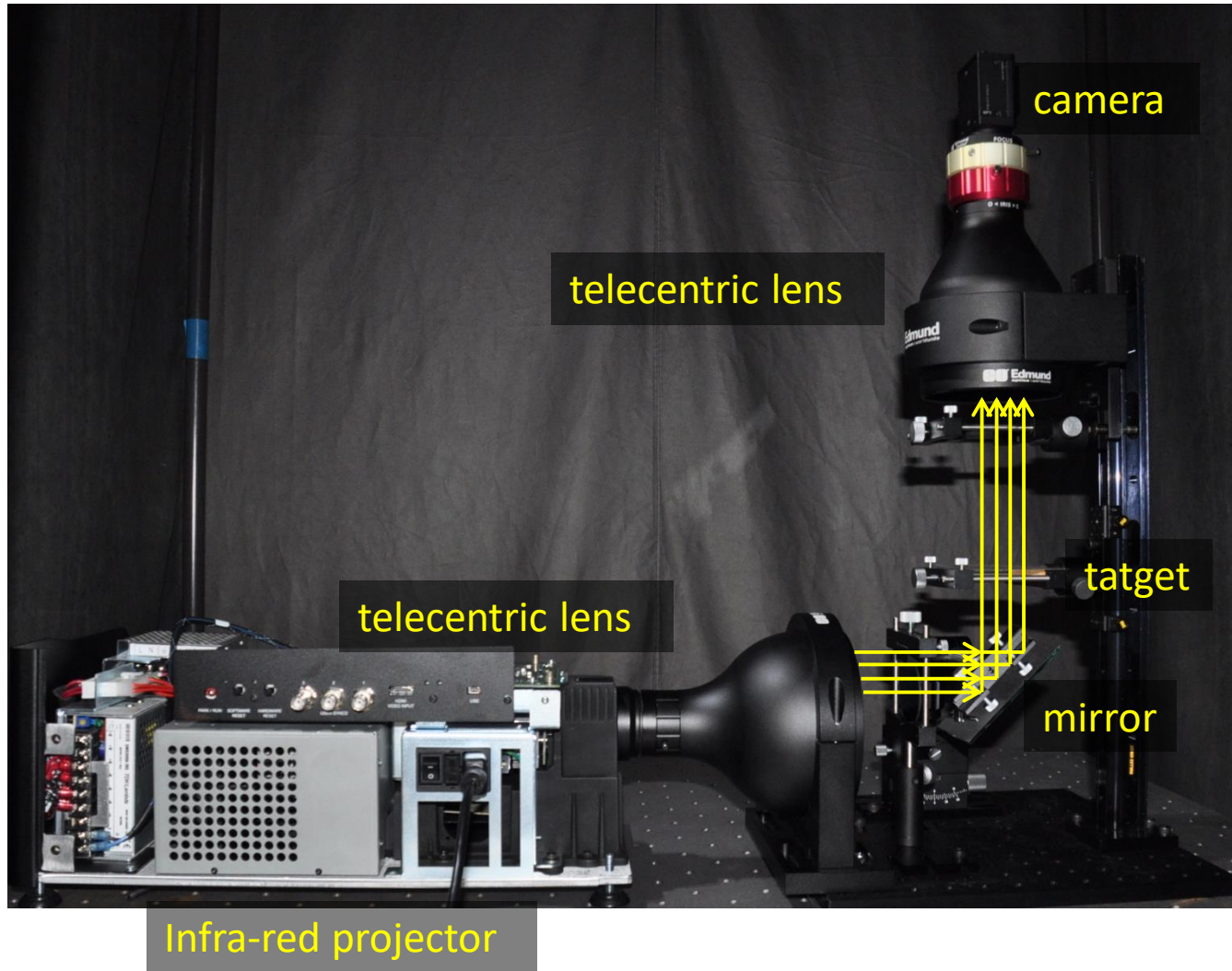
$$min = \frac{1}{2} scattered$$

$$transmissive = max - min$$

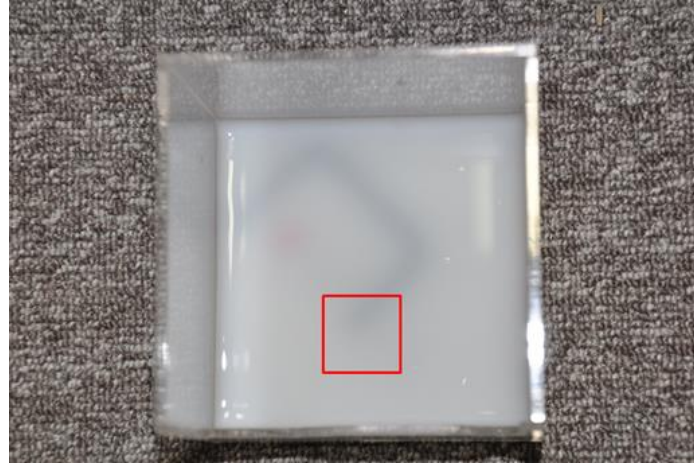
$$scattered = 2 \times min$$



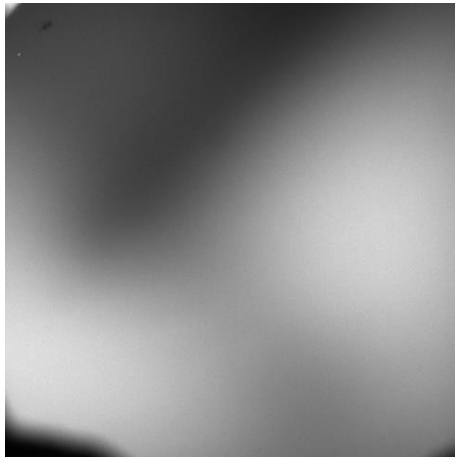
# Overview



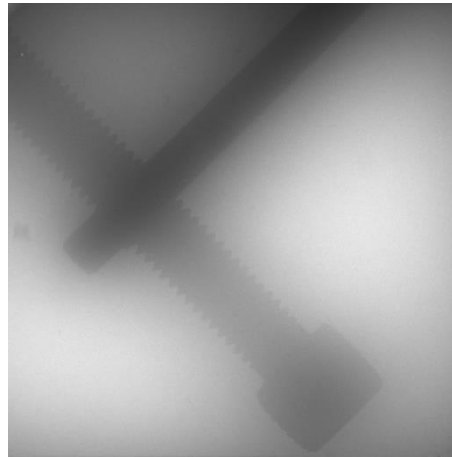
# Transmissive images



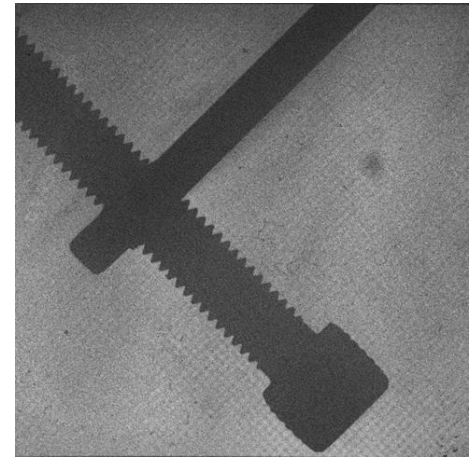
Metal object in murky water



Normal image with visible light

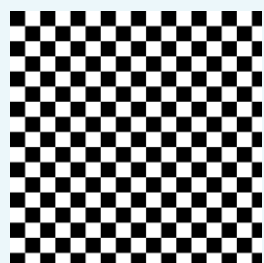


Infra-red image

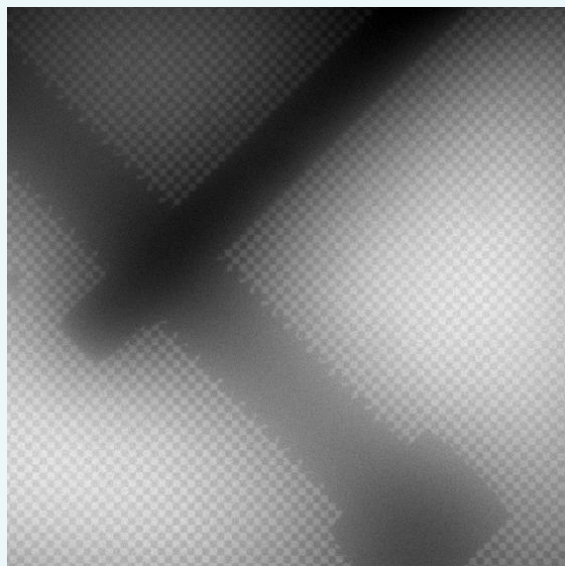


Descattered image

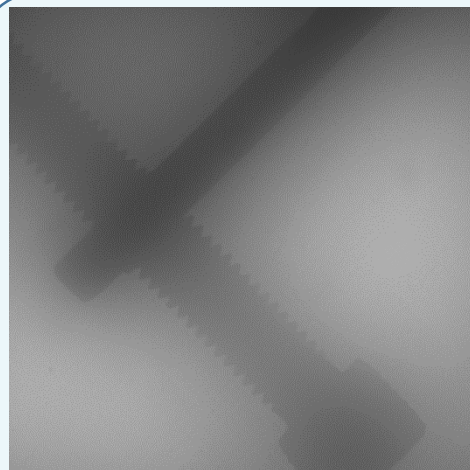
# Process of the descattering



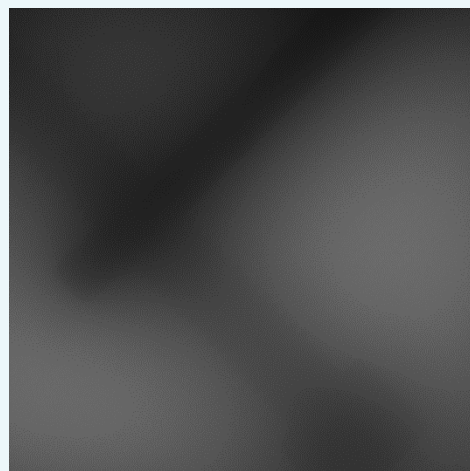
Illumination



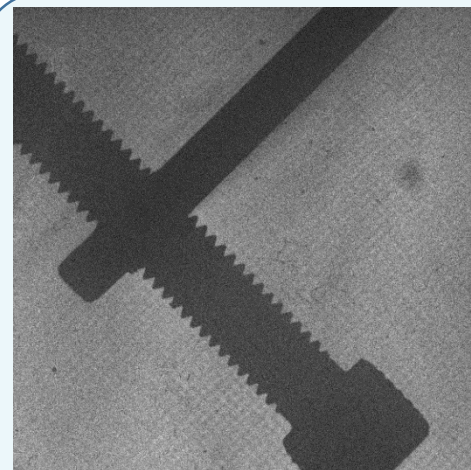
Captured images



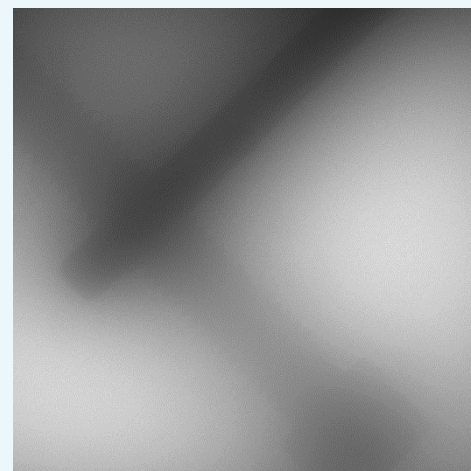
Max



Min



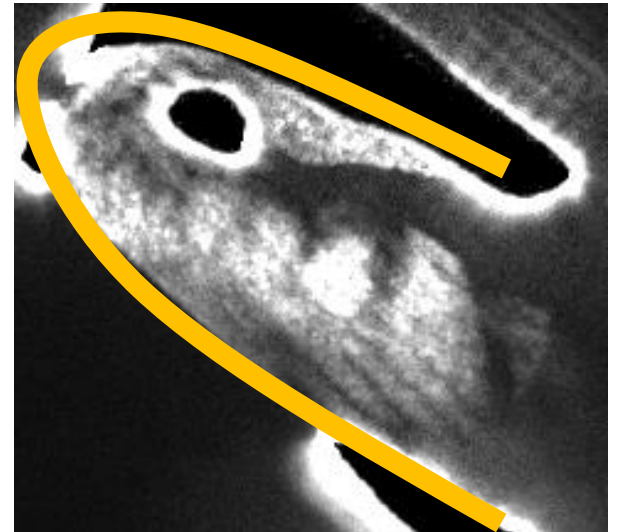
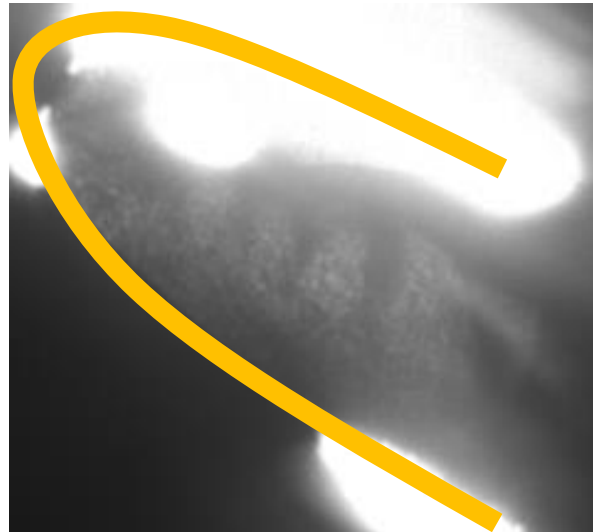
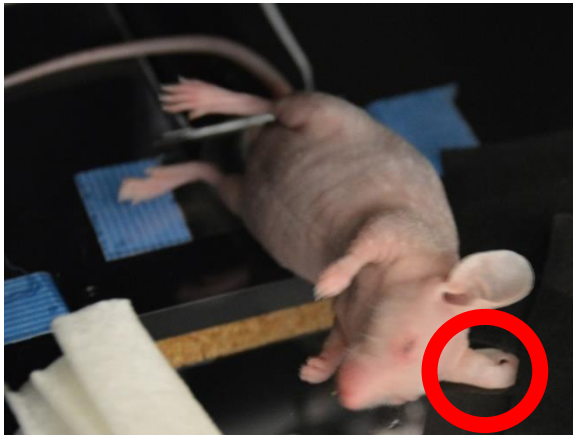
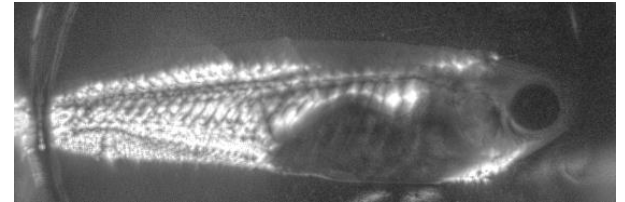
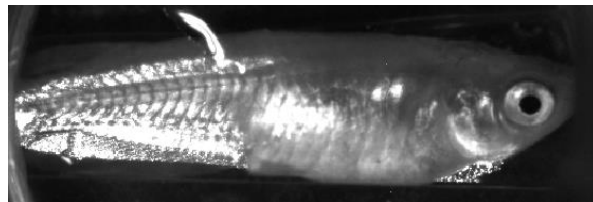
Transmissive



Scattering

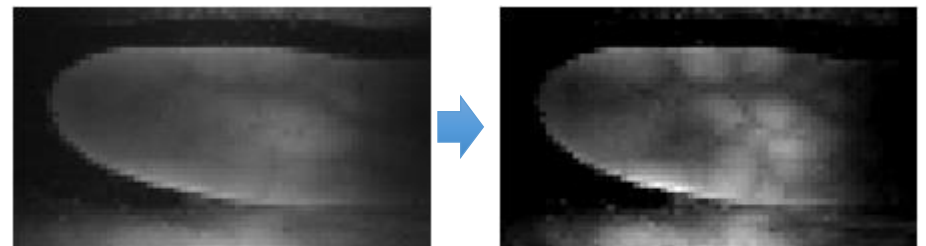
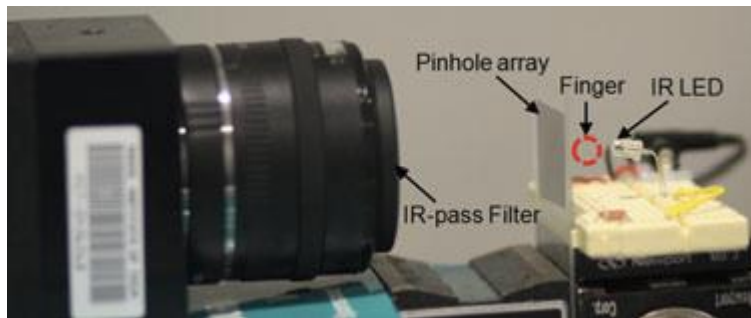
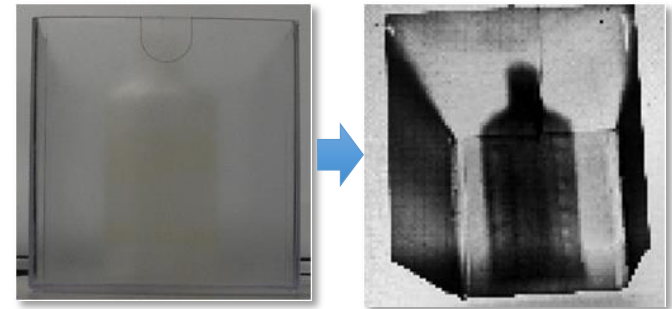
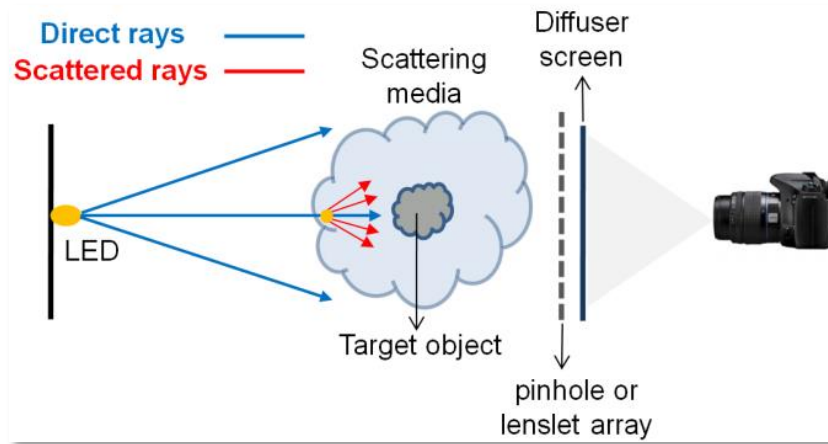
# Application for Bioimaging

## ■ Fish and mouse



# Light field camera for descattering (ECCV2010)

- Light field camera to record spatial  $(x, y)$  and angular  $(\theta, \phi)$  information of rays



Clear vein pattern using NIR light

# Summary of global Illumination

- In our daily environment, there are a lot of volume scattering and subsurface scattering
- In particular, it is difficult to analyze scattering on inhomogeneous materials
- Perfect photometric modeling of real scene is extremely difficult



candle



marble



# Report

■ What is the difference of direct and global components?  
Explain from the following viewpoints.

- Optical phenomena (光学現象)
- Spatial frequency (空間的な周波数)
- Simplicity for modeling (モデル化の容易さ)



Direct component



Global component